

Momento angular orbital de un haz luminoso: Generacion, Deteccion y Aplicaciones.

Jornadas Cientificas 2014, Bucaramanga,

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Noviembre 28, 2014





Contenido

- Momento angular de un haz luminoso.
- Generación de un haz con MAO.
- Detección de un haz con MAO.
- Aplicaciones de un haz con MAO.

Momento angular Orbital de la luz

PHYSICAL REVIEW A

VOLUME 45, NUMBER 11

1 JUNE 1992

Orbital angular momentum of light and the transformation of Laguerre-Gaussian laser modes

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(Received 6 January 1992)



Como se calcula el MAO de un campo EM

Partiendo de las ecuaciones de Maxwell,

$$\left\{ \begin{array}{l} \nabla \cdot \vec{E} = 0 \\ \nabla \cdot \vec{B} = 0 \\ \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \nabla \times \vec{B} = \epsilon_0 \mu_0 \frac{\partial \vec{E}}{\partial t} \end{array} \right\} \rightarrow (\nabla^2 + k^2) \begin{pmatrix} \vec{E} \\ \vec{B} \end{pmatrix} = \vec{0} \mapsto (\nabla^2 + k^2) \begin{pmatrix} \vec{r} \cdot \vec{E} \\ \vec{r} \cdot \vec{B} \end{pmatrix} = \vec{0}.$$

Utilizando:

$$\vec{B} = \sum_{l,m} \left(a_{E(l,m)} f_l(kr) \vec{r}_{l,m} - \frac{i}{\omega} a_{M(l,m)} \nabla \times g_l(kr) \vec{r}_{l,m} \right)$$

$$\vec{E} = \sum_{l,m} \left(\frac{ic^2}{\omega} a_{E(l,m)} \nabla \times f_l(kr) \vec{r}_{l,m} + a_{M(l,m)} g_l(kr) \vec{r}_{l,m} \right),$$

siendo $a_E(l, m)$ y $a_M(l, m)$ coeficientes multipolares, ademas usando

$$u = \frac{1}{2} \left(\epsilon_0 E^2 + \frac{1}{\mu_0} B^2 \right) \quad \vec{j} = \frac{1}{\mu_0} (\vec{r} \times (\vec{E} \times \vec{B}^*)),$$

Se concluye para estado m , la luz transporta Momento angular como

$$\frac{J^{(c)2}}{U^2} = \frac{m^2}{\omega^2} \xleftarrow{N \text{ grande}} \frac{J^{(q)2}(N)}{U^2(N)} = \frac{Nm^2 + Nl(l+1) - m^2}{N\omega^2}.$$

De las expresiones clásicas de los campos EM:

$$\left\{ \begin{array}{l} \vec{E} = -\nabla\Phi - \frac{\partial\vec{A}}{\partial t} \\ \vec{B} = \nabla \times \vec{A} \end{array} \right\} \mapsto \nabla \cdot \vec{A} = 0 \text{ y } \Phi = 0 \mapsto \left\{ \begin{array}{l} \vec{E} = -\frac{\partial\vec{A}}{\partial t} \\ \vec{B} = \nabla \times \vec{A} \end{array} \right\}$$

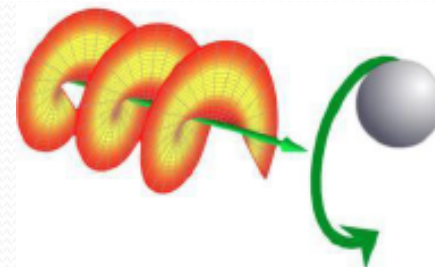
Se obtiene clásicamente que la i -ésima componente de Momento angular del haz es

$$J_i = \underbrace{\frac{1}{\mu_0} \epsilon_{ijk} \int A_j \dot{A}_k d^3r}_{MAS} + \underbrace{\frac{1}{\mu_0} \int \epsilon_{ijk} x_j \partial_k (\dot{A}_p) \dot{A}_p d^3r}_{L_i} \longrightarrow \vec{J} = \vec{S} + \vec{L},$$

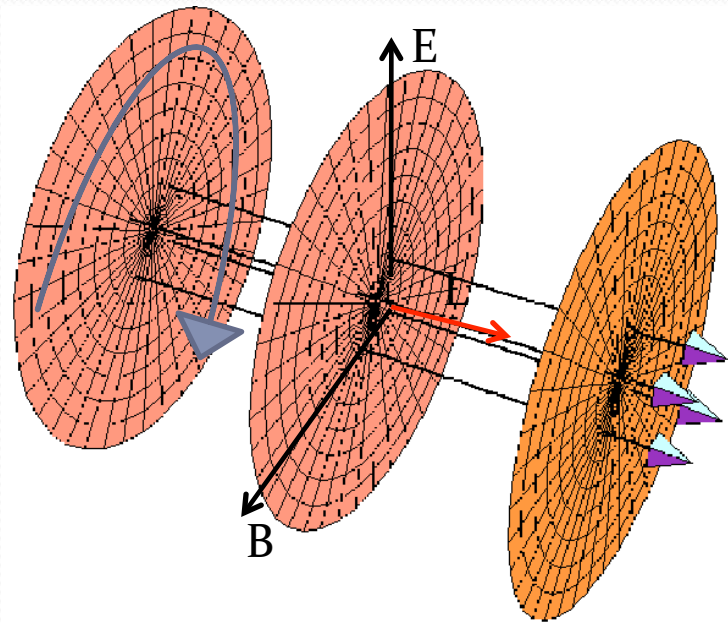
MAO

mientras cuánticamente la i -ésima componente de Momento angular del haz es

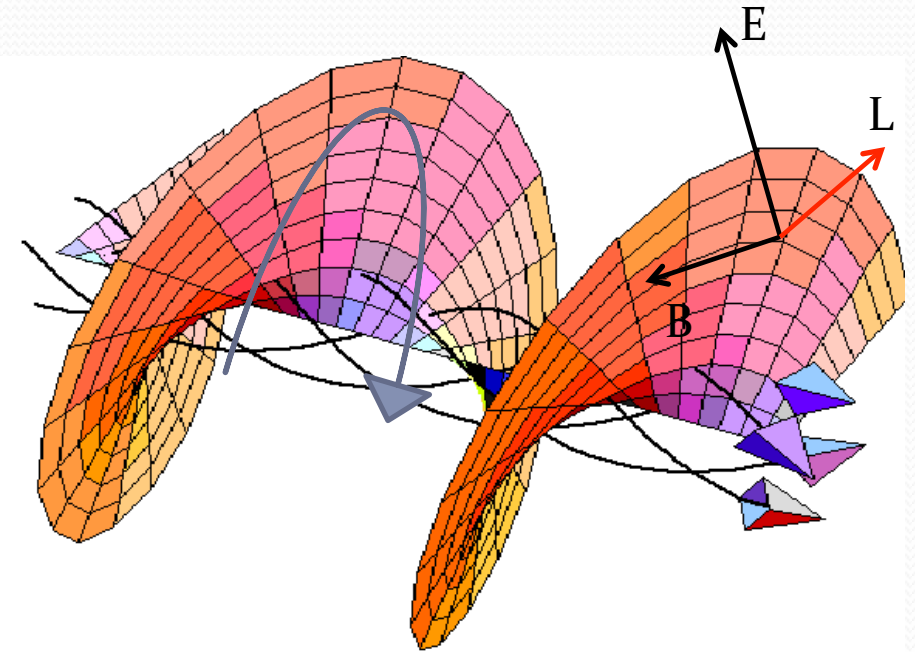
$$\hat{J}_i = \underbrace{\frac{1}{\mu_0} \int \hat{E}_j^* \underbrace{(-i\epsilon_{ijk})}_{\hat{S}_i} \hat{E}_k d^3r}_{MAS} + \underbrace{\frac{1}{\mu_0} \int \hat{E}_j^* \underbrace{(-i\hat{r} \times \hat{\nabla})_i}_{\hat{L}_i} d^3r}_{MAO} \longrightarrow \hat{J} = \hat{S} + \hat{L}.$$



Momento angular Orbital de la luz

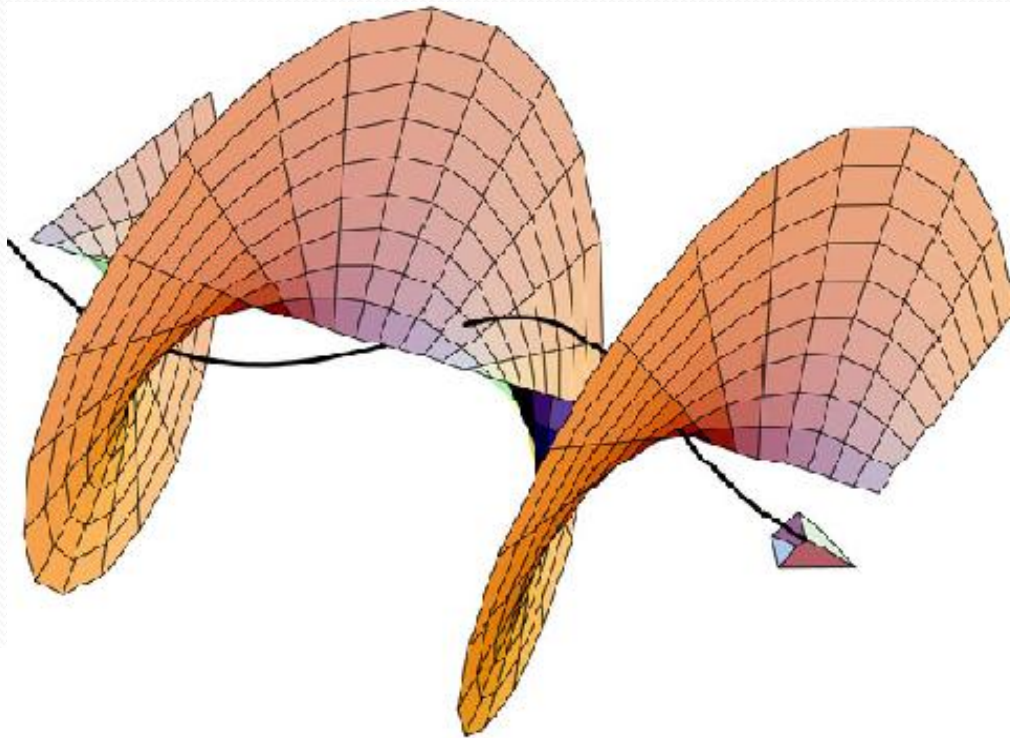


$L=0$



$L \neq 0$

Momento angular de un haz



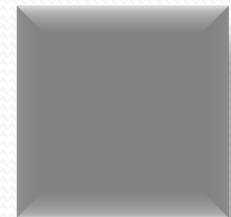
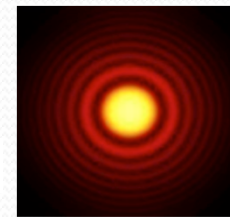
<http://www.gla.ac.uk/schools/physics/research/groups/optics/research/orbitalangularmomentum/>

Fase, $2\pi \geq \theta \geq 0$.

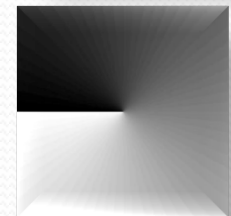
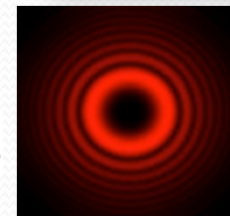
$$\phi = m\theta.$$

Intensidad, $I \geq 0$.

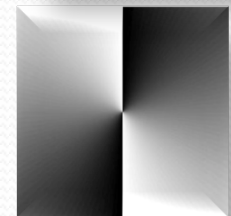
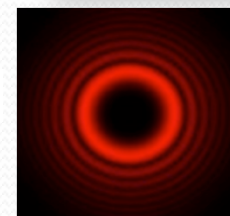
$m = 0$



$m = 1$



$m = 2$

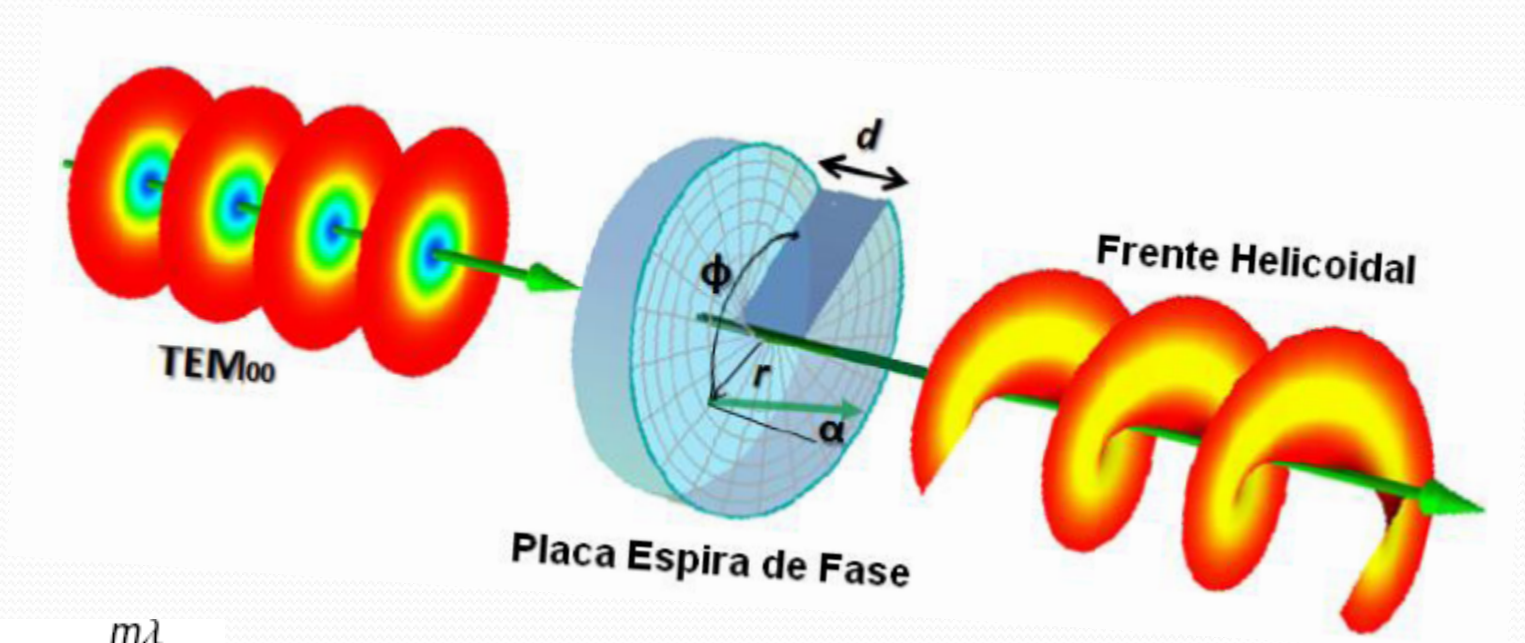


I

ϕ

. Generación de Haces con MAO

- Placas de espiral de Fase



Con

$$d = \frac{m\lambda}{(n_1 - n_2)}.$$

Fase introducida y MAO

$$\delta = \frac{(n_1 - n_2)d}{\lambda} \phi, \quad \text{y} \quad \boxed{L_z \approx m\hbar}$$



1 December 1994

Optics Communications 112 (1994) 321-327

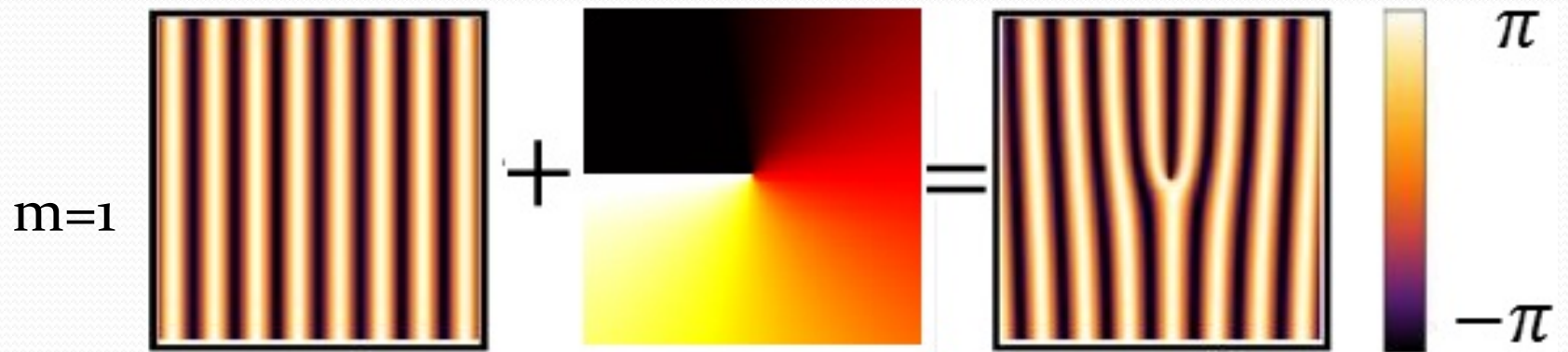
OPTICS
COMMUNICATIONS

Helical-wavefront laser beams produced with a spiral phaseplate

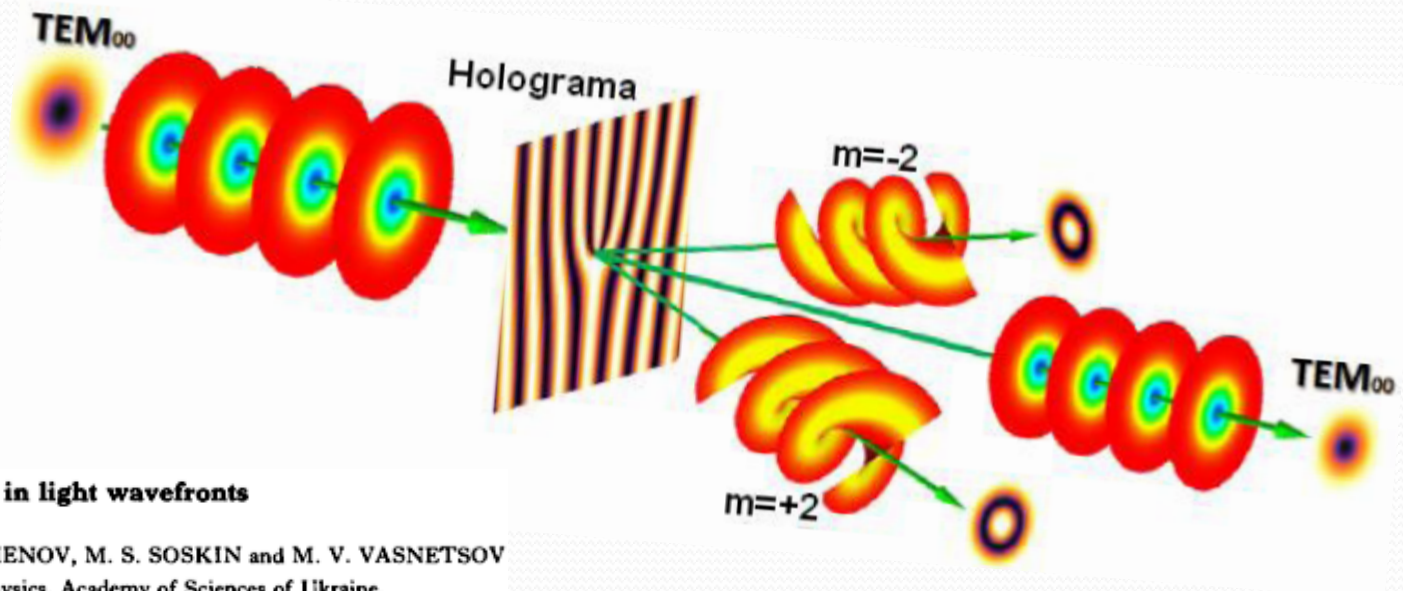
M.W. Beijersbergen, R.P.C. Coerwinkel, M. Kristensen¹, J.P. Woerdman
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Received 30 August 1994

- Hologramas en forma de tenedor



Luego,



Screw dislocations in light wavefronts

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252650 Kiev, Prospect Nauki 46, Ukraine

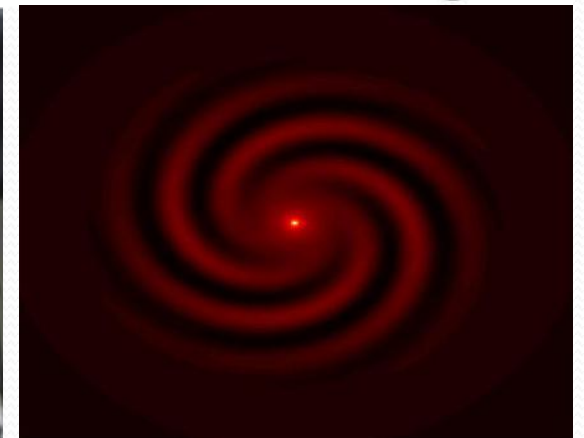
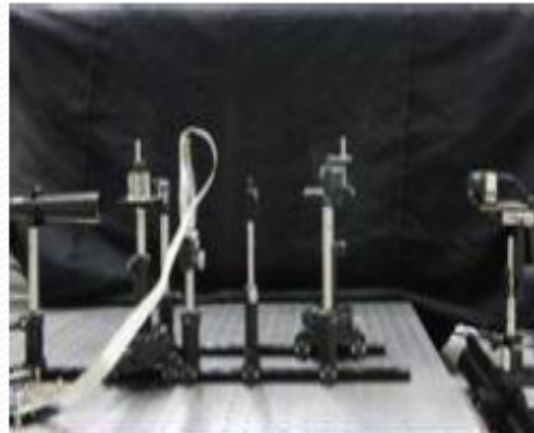
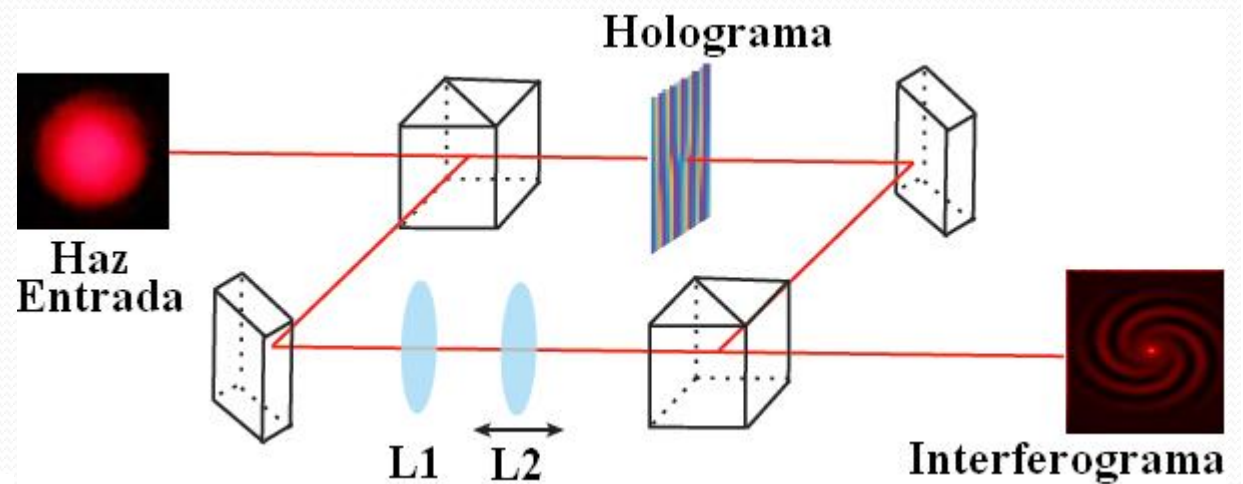
(Received 14 June 1991; revision received 8 January 1992)

Detección de haces con MAO

- Interferometría

El numero de espirales es igual a la 2m.

- Es para muchos fotones.



Intensity of a beam with integer and non-integer charge angular orbital momentum in far field

Cristian Hernando Acevedo Cáceres*

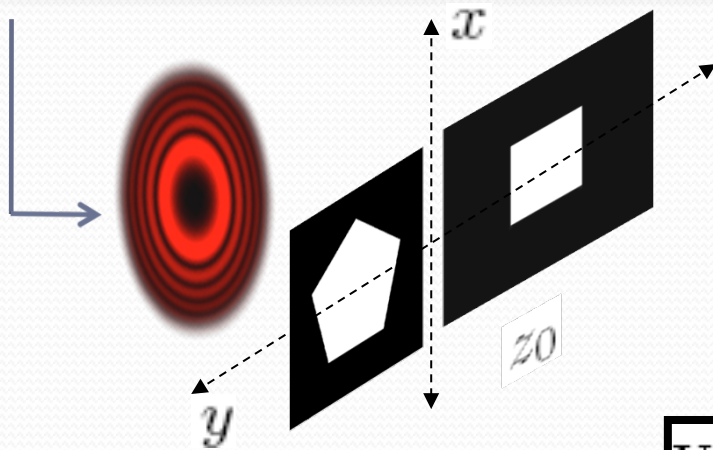
Carlos Fernando Díaz Meza**

Yezid Torres Moreno***

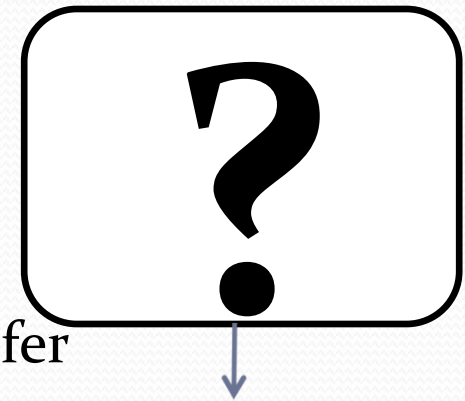
Universidad Industrial de Santander (Colombia)

- Difracción a través de aperturas

$$U(\rho, \theta, z_0) = c_0 e^{-\frac{\rho^2}{2w^2(z_0)}} e^{im\theta} \rho \left[I_{\frac{m-1}{2}} \left(\frac{\rho^2}{2w^2(z_0)} \right) - I_{\frac{m+1}{2}} \left(\frac{\rho^2}{2w^2(z_0)} \right) \right]$$



Difracción de Fraunhofer



$$U(r, \varphi, z) = f(z) [(-i)^m e^{im\varphi} H_n \{U_\rho(\rho)\}]_{r \rightarrow r/\lambda(z-z_0), \theta \rightarrow \varphi}$$

con

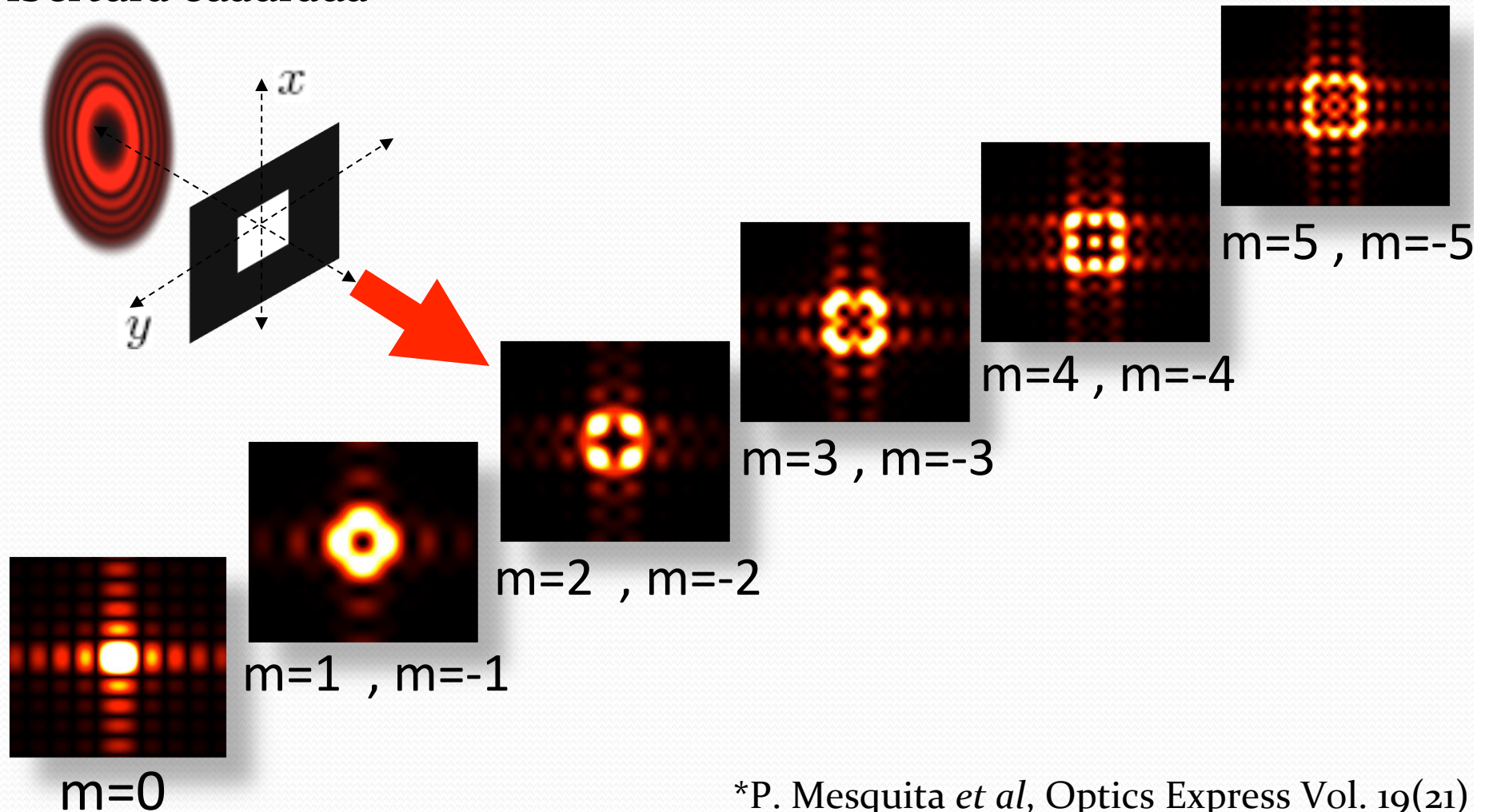
$$H_n \{U_\rho(\rho)\} = 2\pi c_0 \int \rho^2 t(\rho) e^{-\frac{\rho^2}{2w^2(z_0)}} \left[I_{\frac{m-1}{2}} \left(\frac{\rho^2}{2w^2(z_0)} \right) - I_{\frac{m+1}{2}} \left(\frac{\rho^2}{2w^2(z_0)} \right) \right] J_m(2\pi r \rho) d\rho.$$

DETERMINACIÓN DE LA CARGA TOPOLÓGICA DE UN HAZ BESSEL MEDIANTE
EL PATRÓN DE DIFRACCIÓN A TRAVÉS DE UNA RENDIJA TRIANGULAR
EQUILÁTERA

Cristian Hernando Acevedo, Carlos Fernando Díaz y Yezid Torres Moreno.

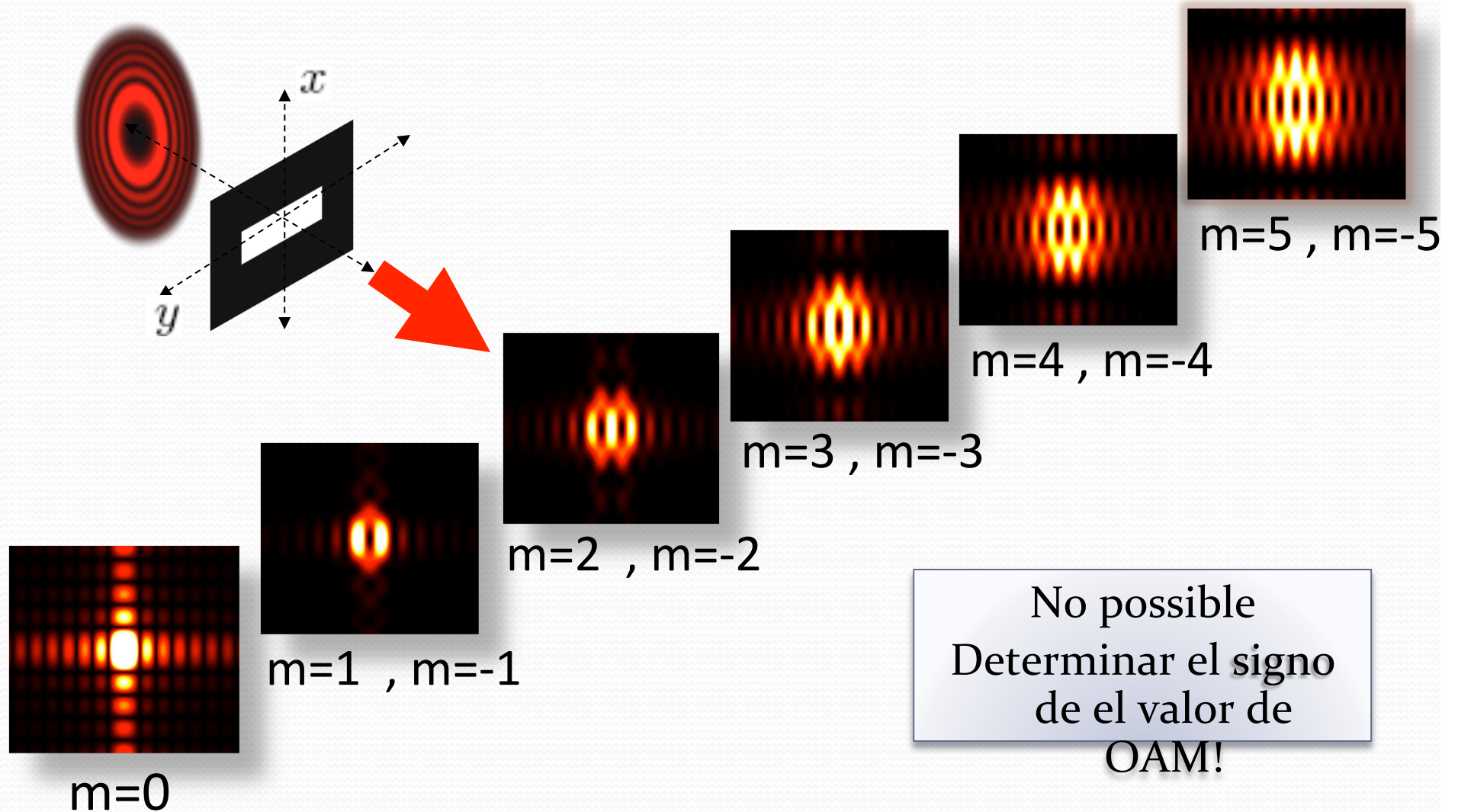
Resultados Numéricos

- Abertura cuadrada*

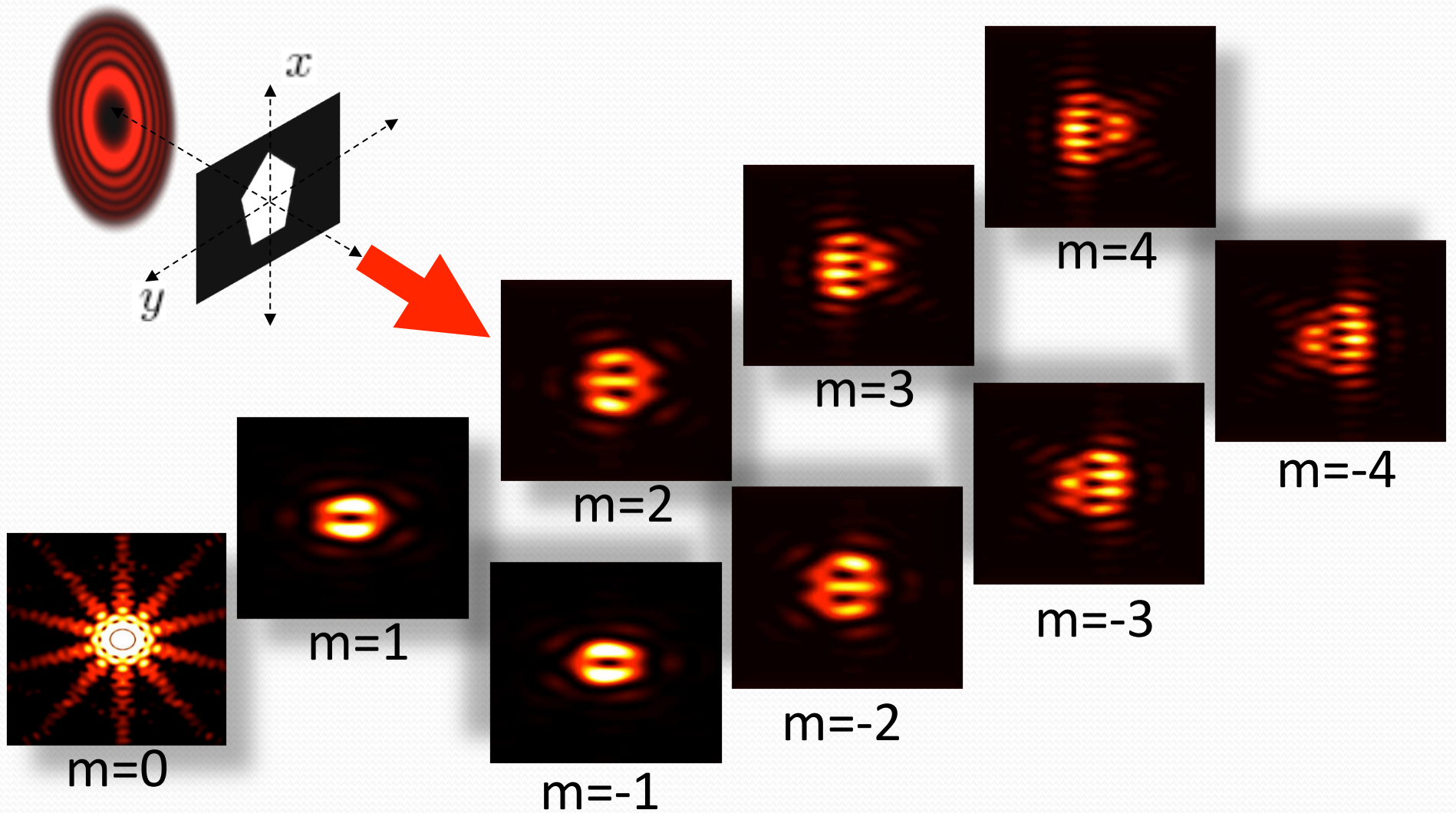


*P. Mesquita *et al*, Optics Express Vol. 19(21)

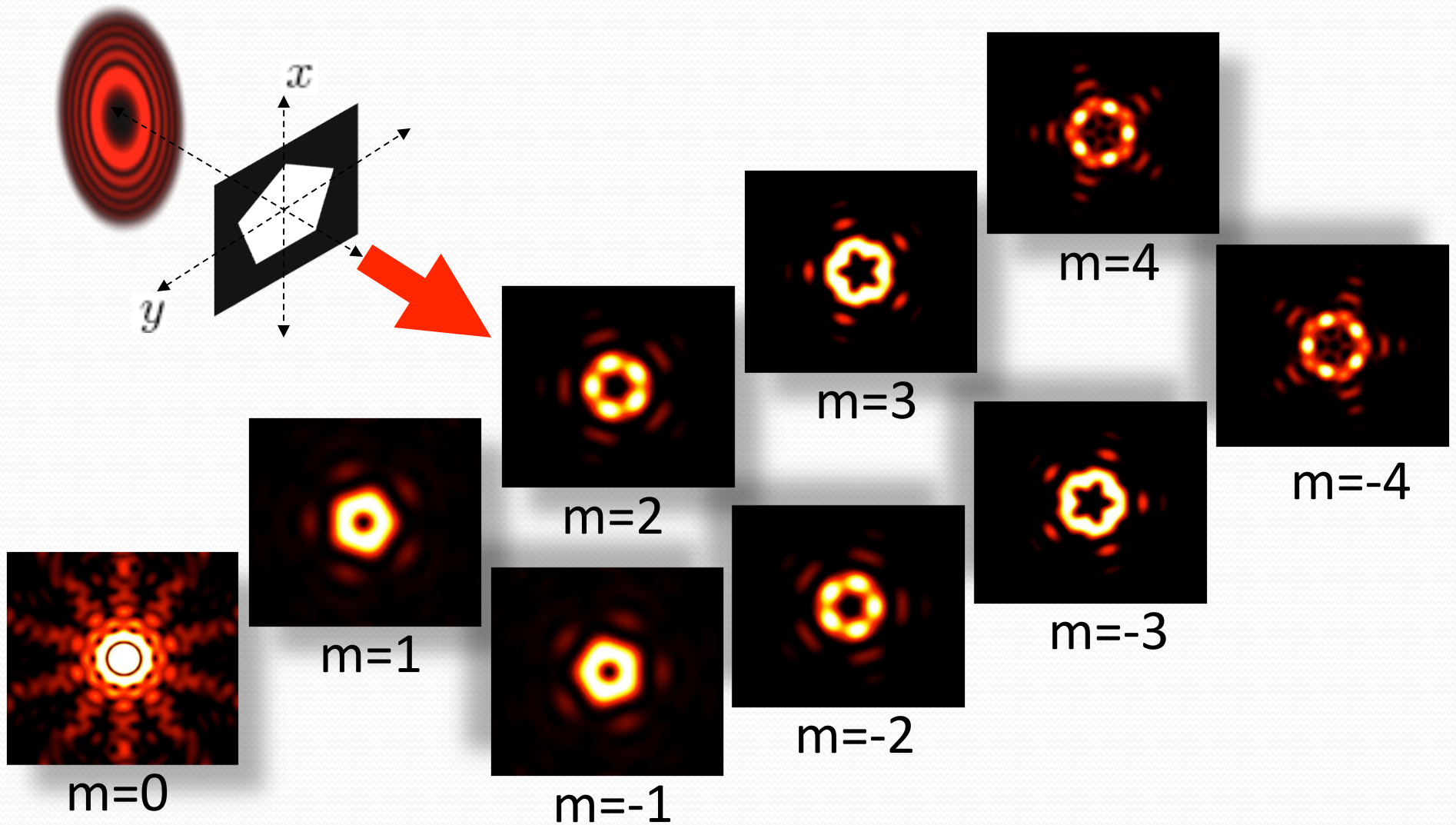
- Abertura rectangular



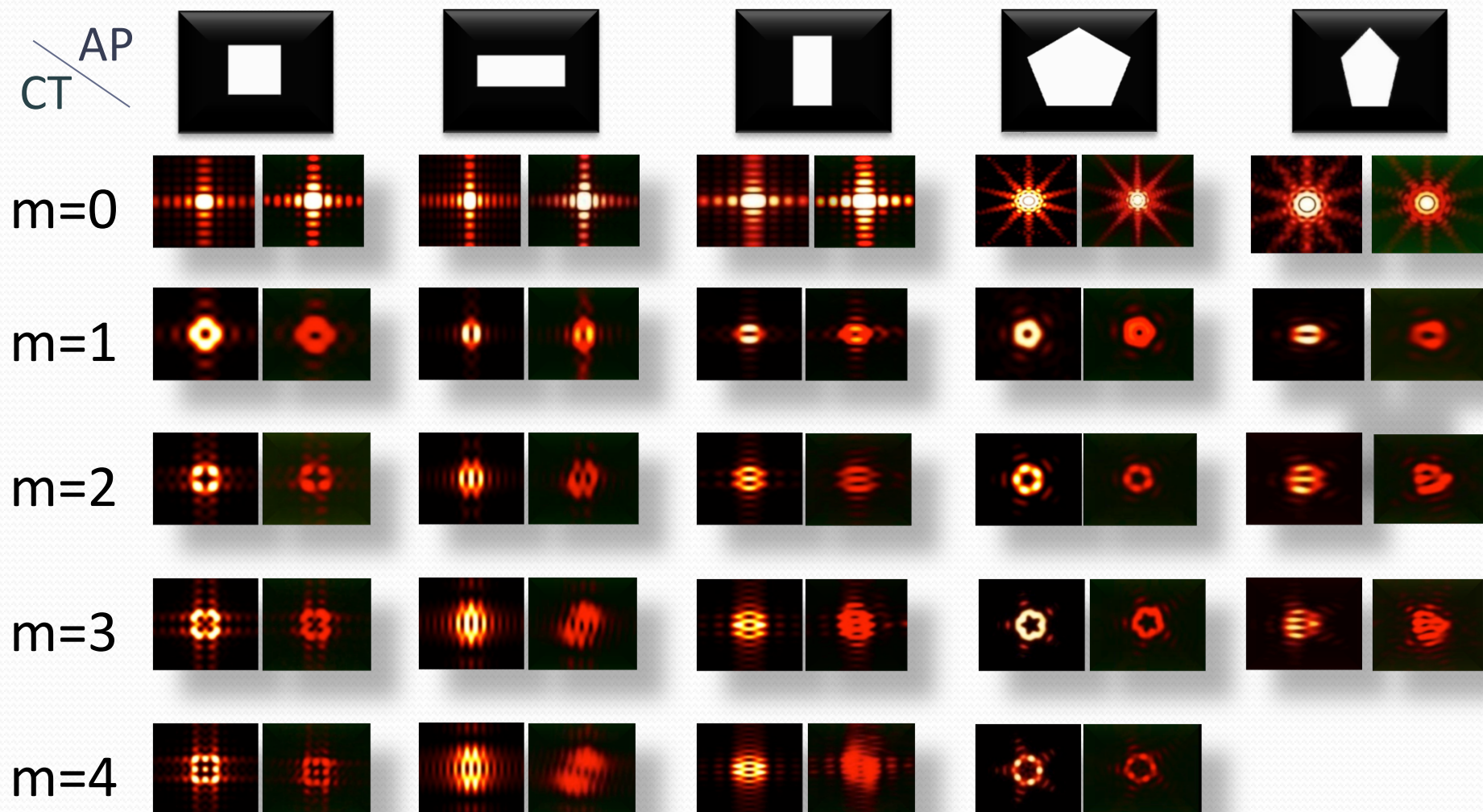
- Abertura pentagonal equilátera



- Abertura pentagonal no equilátera

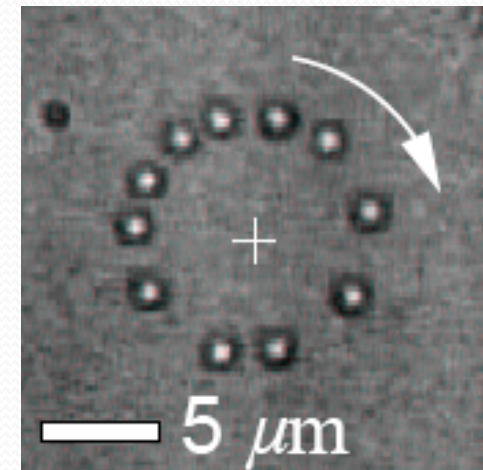
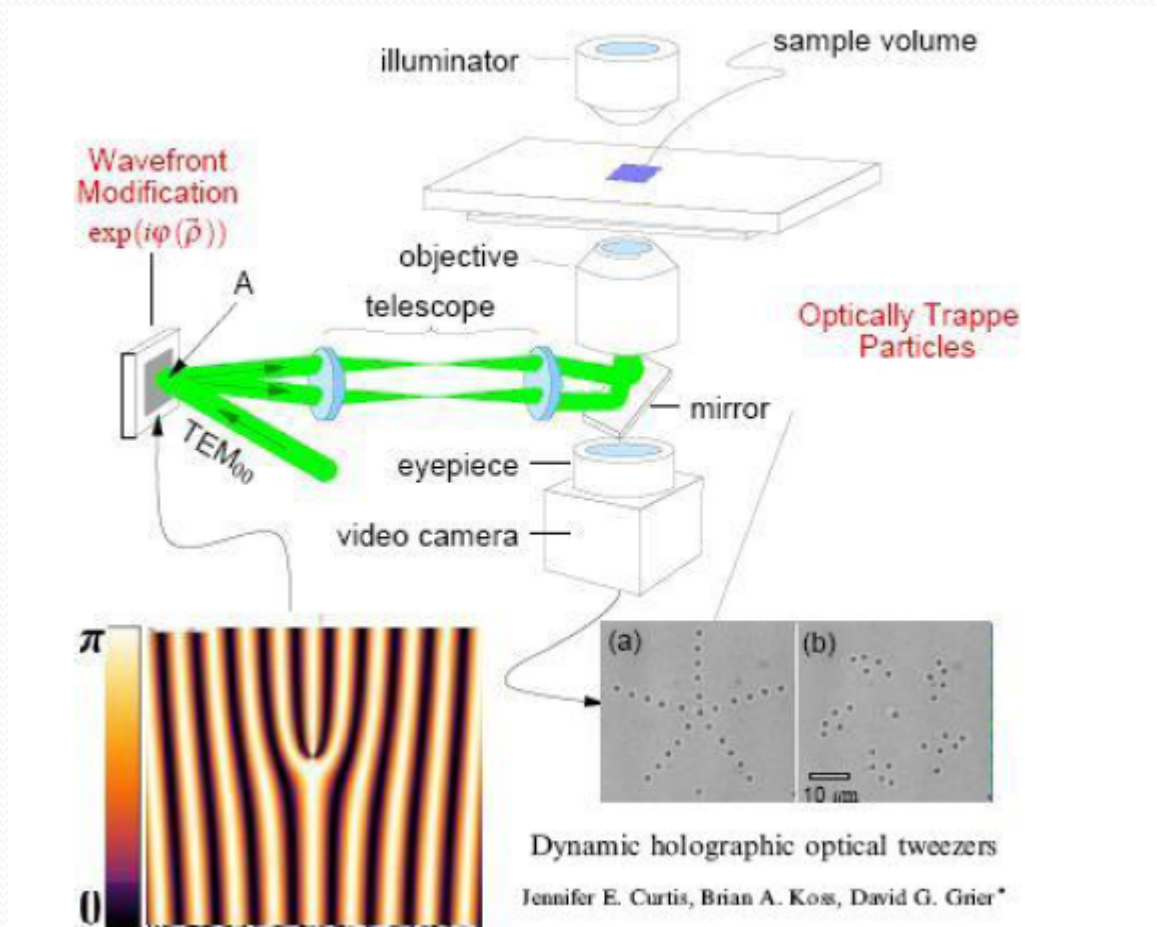


Resultados Generales



Aplicaciones de haces con MAO

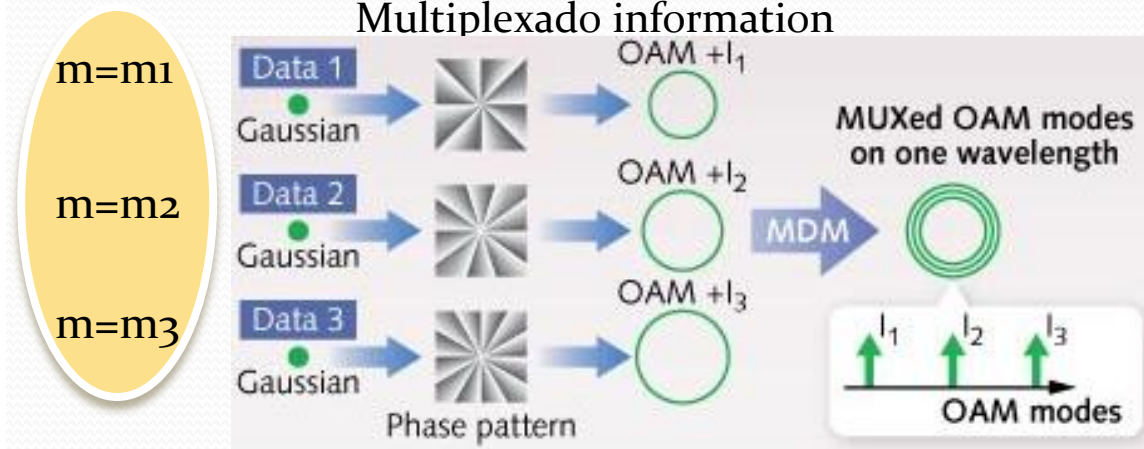
Pinzas Opticas*



* D. Grier and E. Curtis, Physics review letters, Vol . 90(133901)

** P. Marinelli, *et al*, Electronics Letters, Vol. 47(17).

- Codificación de Información

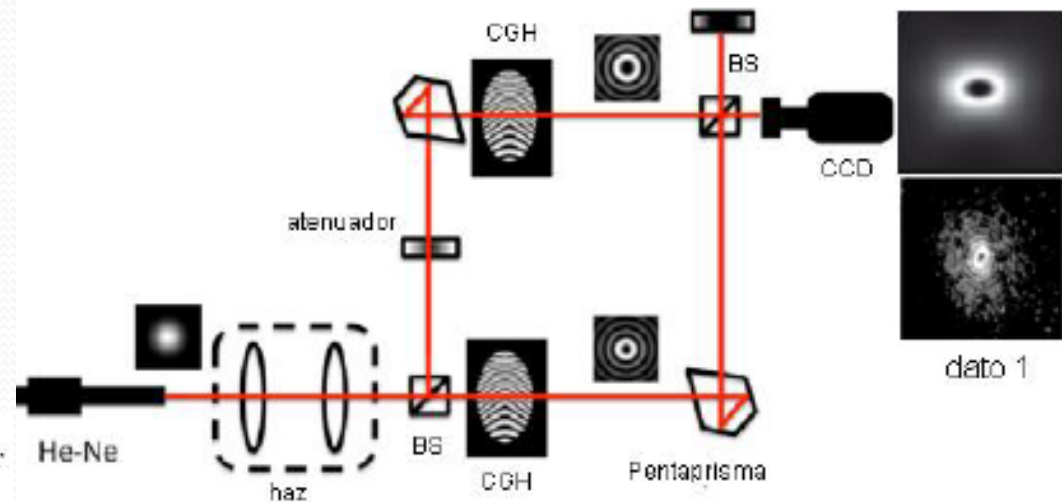


- Es posible codificar al orden de Terabits



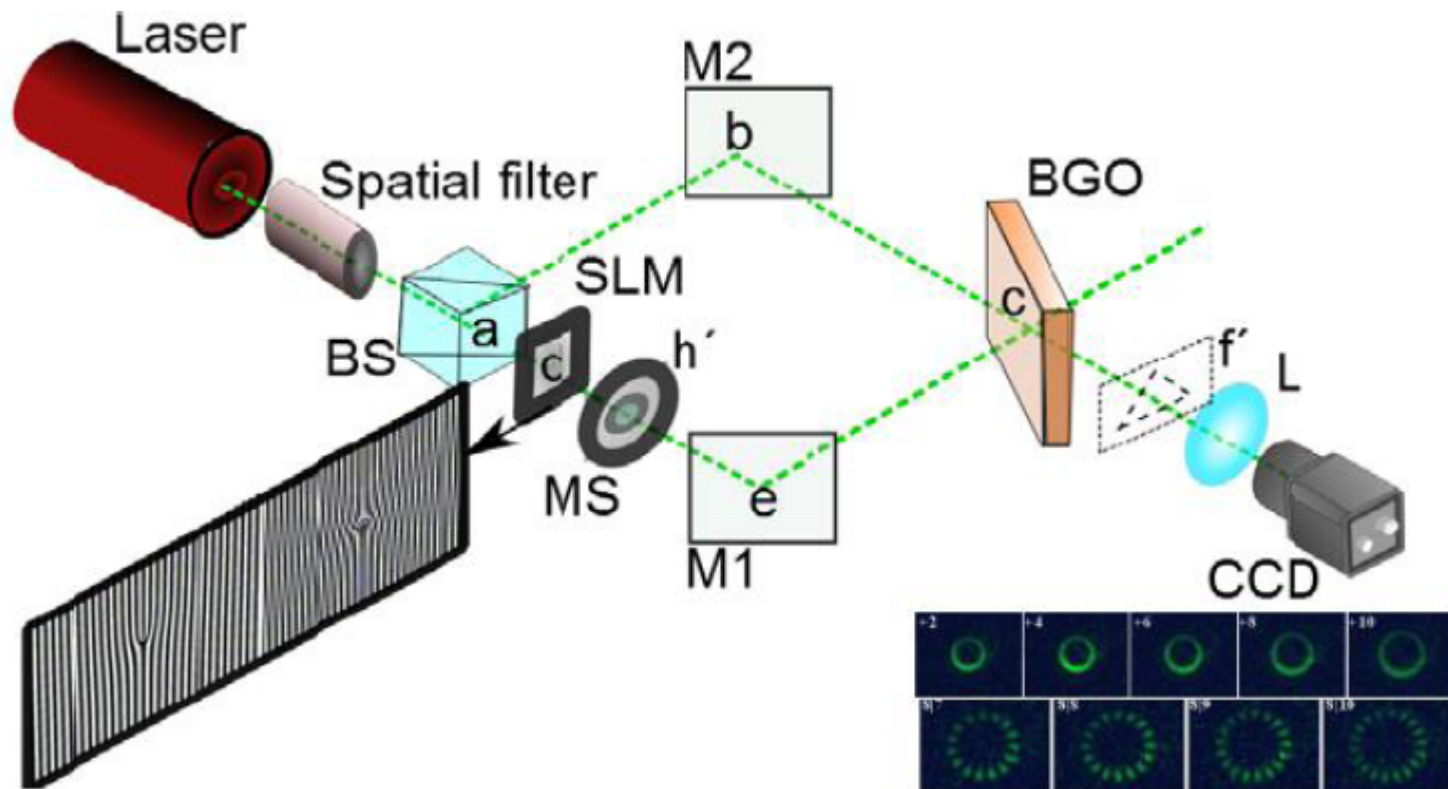
Preliminary Optoelectronic Encoder Modeling for Data Transfer Through the Orbital Angular Momentum of Light

CARLOS FERNANDO DÍAZ MEZA CRISTIAN HERNANDO ACEVEDO CÁCERES YEZID TORRES MORENO
JAIME GUILLERMO BARRERO PÉREZ



Perspectivas*

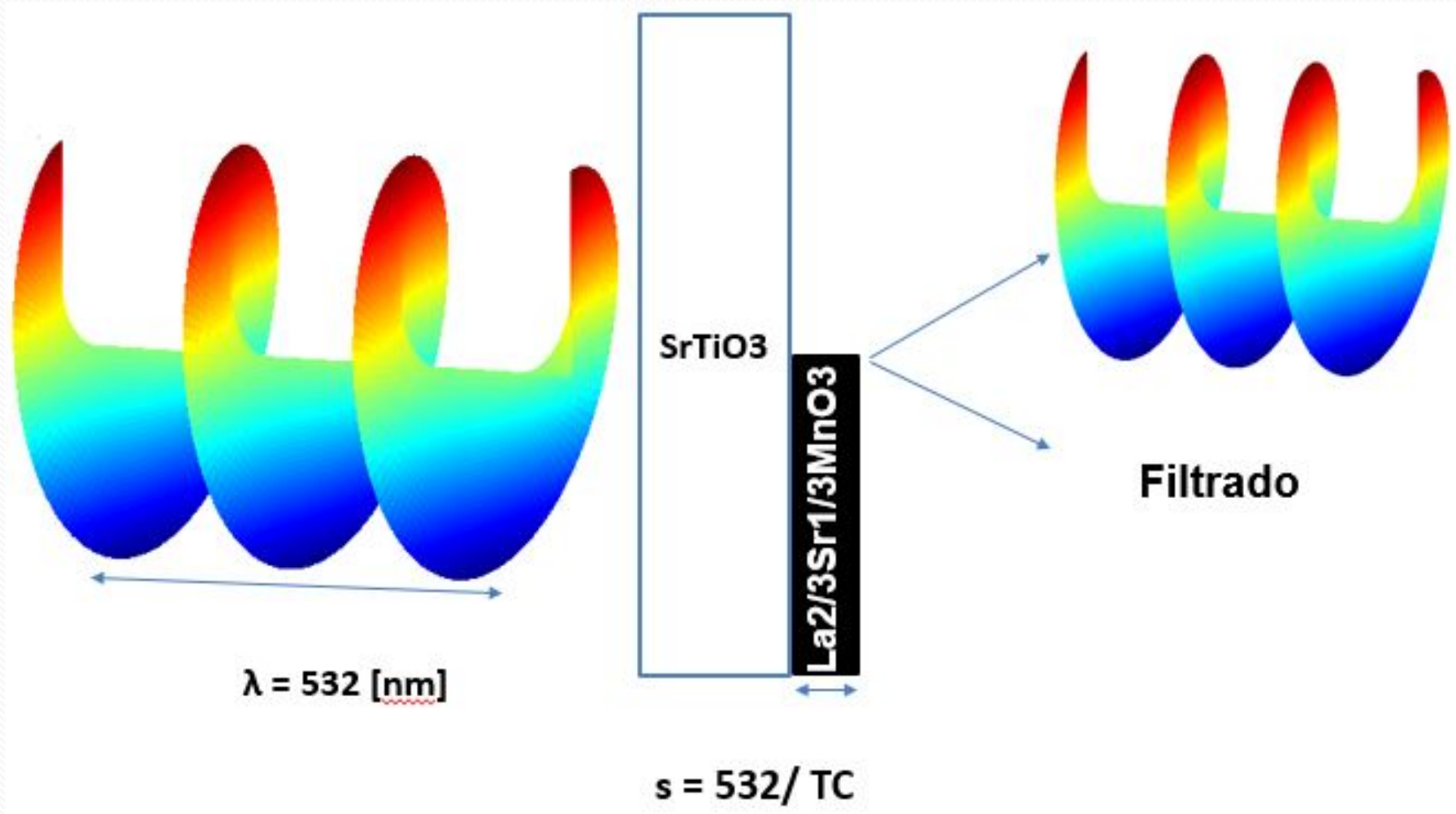
- Compuerta lógica sobre un cristal fotorrefractivo



Recording a Beam with Integer Angular Orbital Momentum into a Photorefractive Crystal BGO

Cristian H. Acevedo^a, Vladimir A. Jerez^a, Carlos F. Diaz^a, Yezid Torres^b and Ángela M. Guzmán^b

- Decodificador usando películas delgadas



Gracias!

PREGUNTAS?



Unidades Financiadoras

